

$$\begin{aligned} \rho u \frac{\partial v}{\partial x} + \rho v \frac{\partial u}{\partial y} + \rho w \frac{\partial v}{\partial z} &= -\frac{\partial p}{\partial y} \\ \frac{\partial}{\partial y} \left(\lambda \nabla \cdot \mathbf{v} + 2\mu \frac{\partial v}{\partial y} \right) + \frac{\partial}{\partial z} \left[\mu \left(\frac{\partial w}{\partial y} + \frac{\partial v}{\partial z} \right) \right] &= E_y + \sqrt{N} Q^{-1} (1 - Pa) \\ = \sqrt{N} [Q^{-1}(P_w) + Q^{-1}(1 - Pa)] &= \sqrt{N} \int_{E_y}^1 \exp(-v^2/2N) dv \\ P_w = \int_{E_y}^1 dP_v &= \frac{1}{\sqrt{2\pi N}} \int_{E_y}^1 \exp(-v^2/2N) dv \end{aligned}$$

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The Pioneer Anomaly and Space Accelerometers for Gravity Tests

Agnès Levy DMPH/IEA

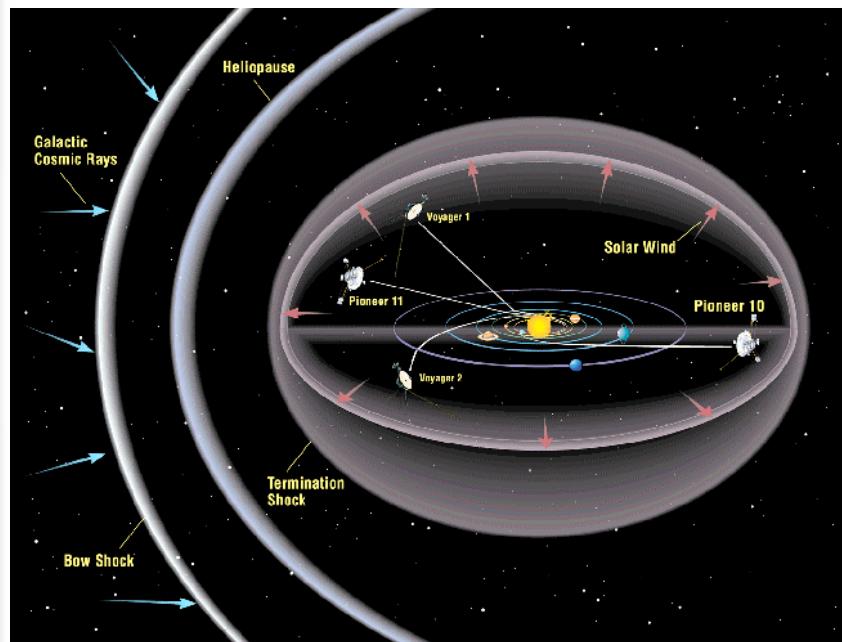
27/06/2006

Office National d'Études
et de Recherches Aérospatiales
www.onera.fr

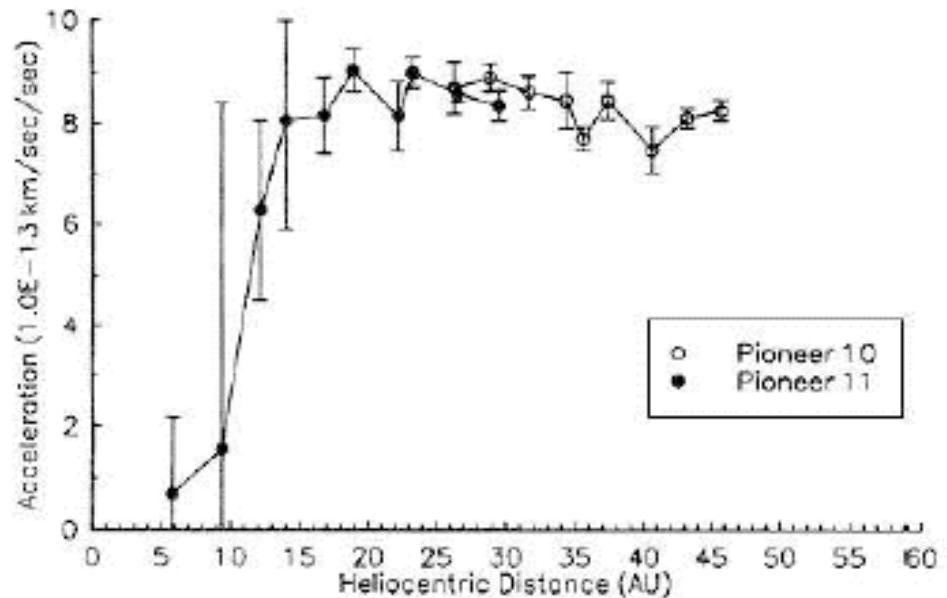
The Pioneer Anomaly

Pioneer 10 launched March 2, 1972
Pioneer 11 launched April 5, 1973

Deceleration : $(8.74 \pm 1.33) 10^{-10} \text{ m.s}^{-2}$



UNMODELED ACCELERATIONS ON PIONEER 10 AND 11
Acceleration Directed Toward the Sun



J. Anderson et al, Phys. Rev. D 65 (2002) 082004

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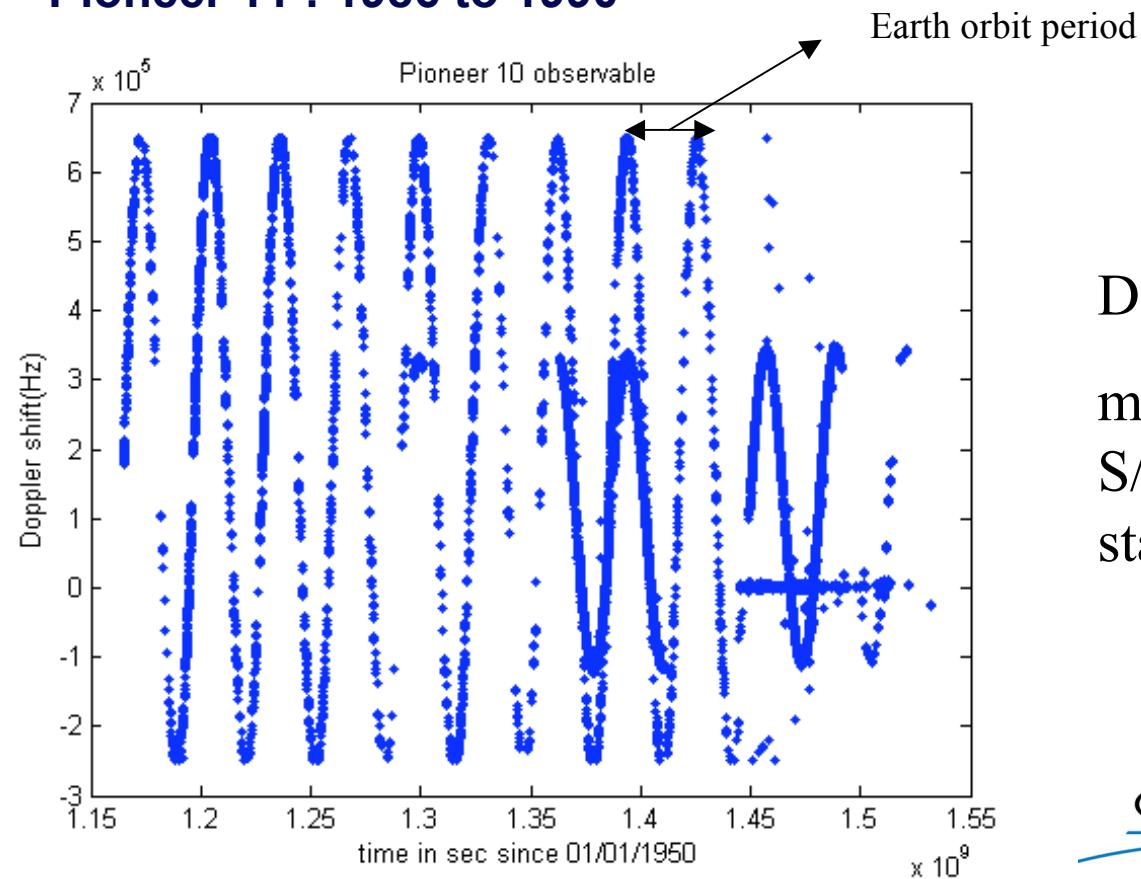
Various aspects of my work

- Trajectory independant analysis : Pioneer anomaly verification
- Telemetry data analysis : study of the more probable source, residual thrust from S/C itself
- Instrument development : adaptation of an ONERA accelerometer for the Pioneer anomaly measurement

Doppler data analysis

► Pioneer 10 and 11 binary ODFs (Orbit Data Files)

- Pioneer 10 : 1987 to 1998
- Pioneer 11 : 1986 to 1990



Doppler shift :
movement of the
S/C wrt to Earth
stations

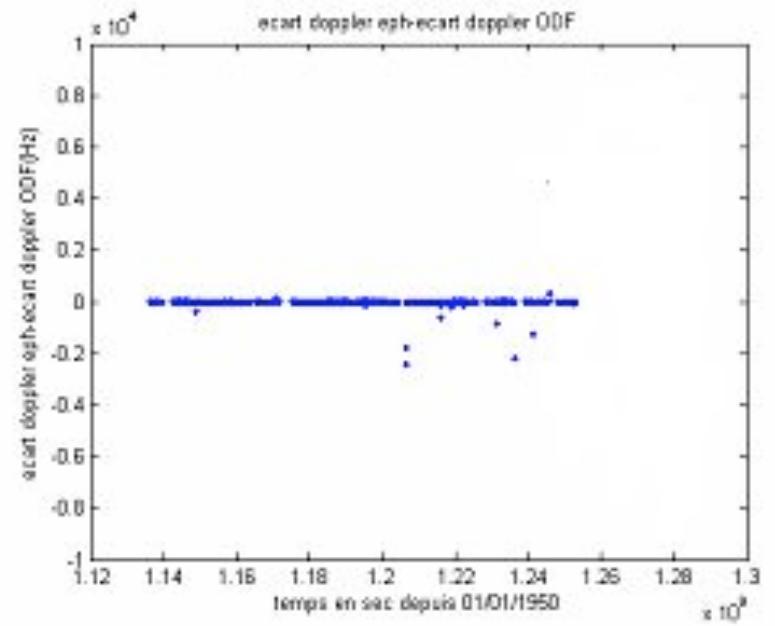
Development of independant software

- Evaluate the doppler shift
 - Develop an overall simulation by using software developed at the Observatoire de la Côte d'Azur
- Comparison to Pioneer measure data
- Simulation of new mission

computed doppler shift

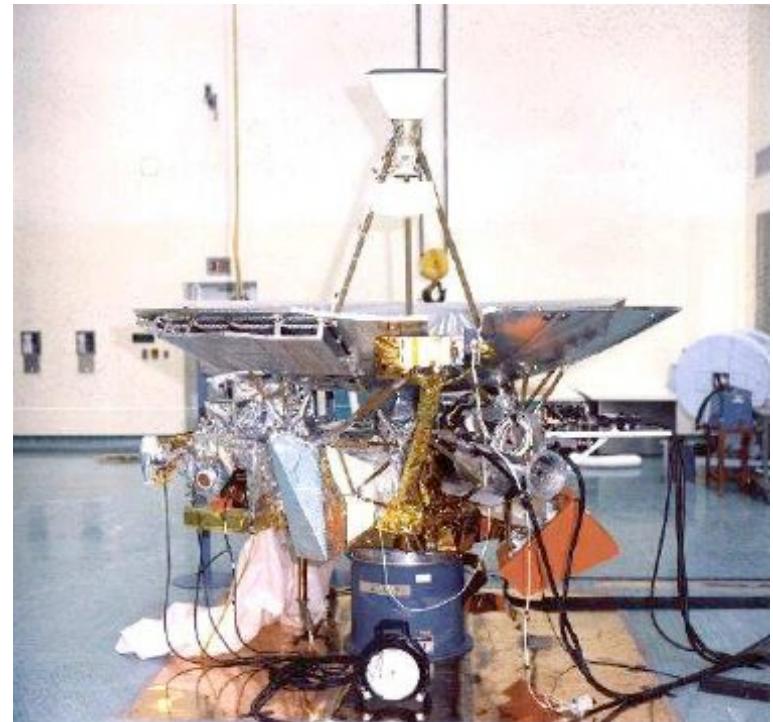
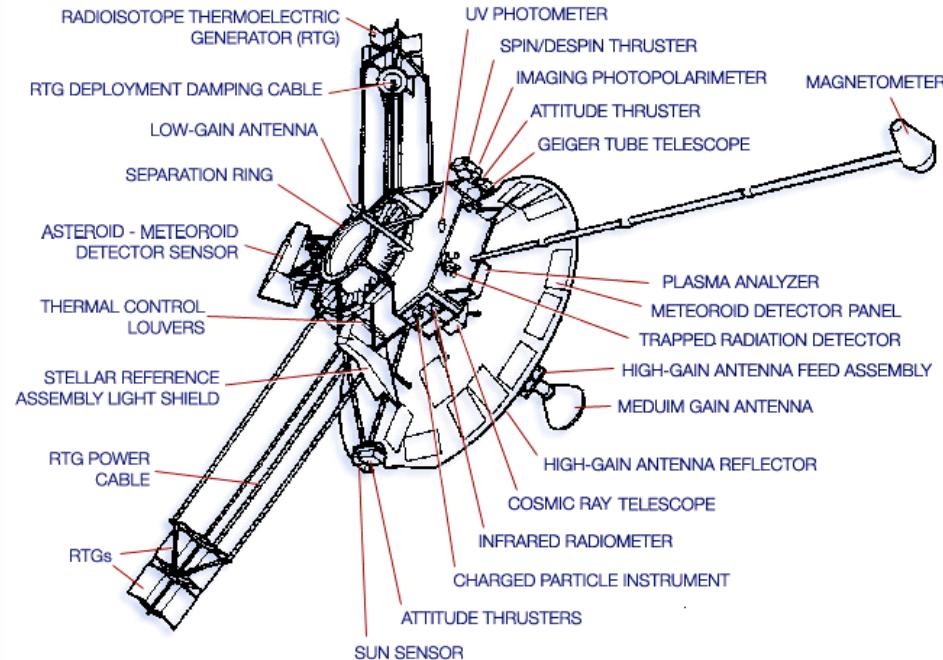


Observation of an anomaly ?

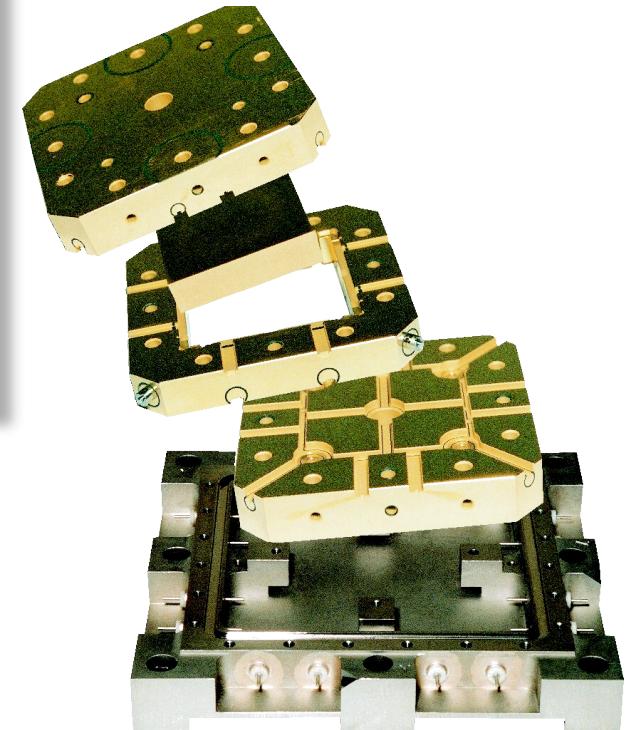
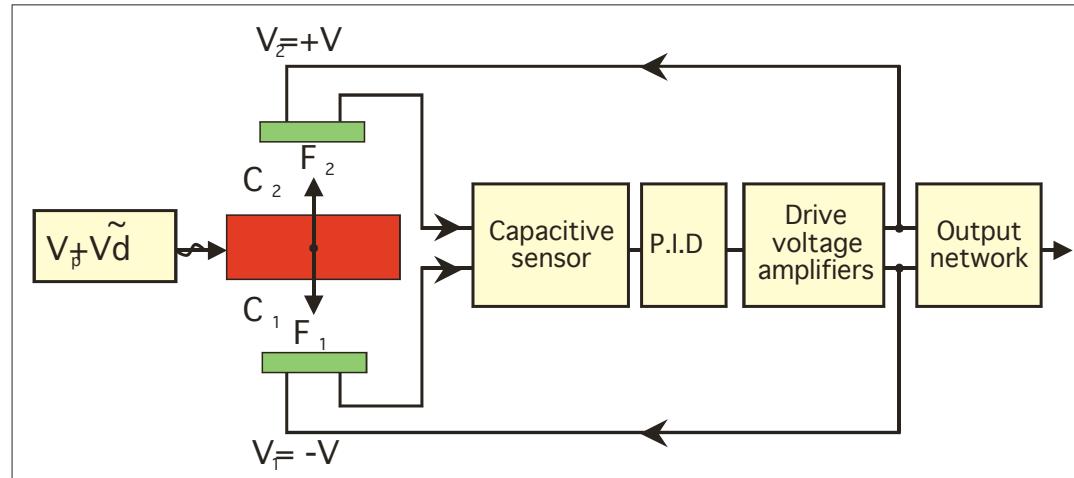


Telemetry data analysis : S/C behaviour

- Test the hypothesis of RTG asymmetric radiation
- Development of a thermo-electrical model
- Modeling of the thermal radiation processes



Space existing electrostatic accelerometer



$$F = F_1 + F_2 = \frac{1}{2} [\nabla C_1 (V_1 - V_p)^2 + \nabla C_2 (V_2 - V_p)^2]$$

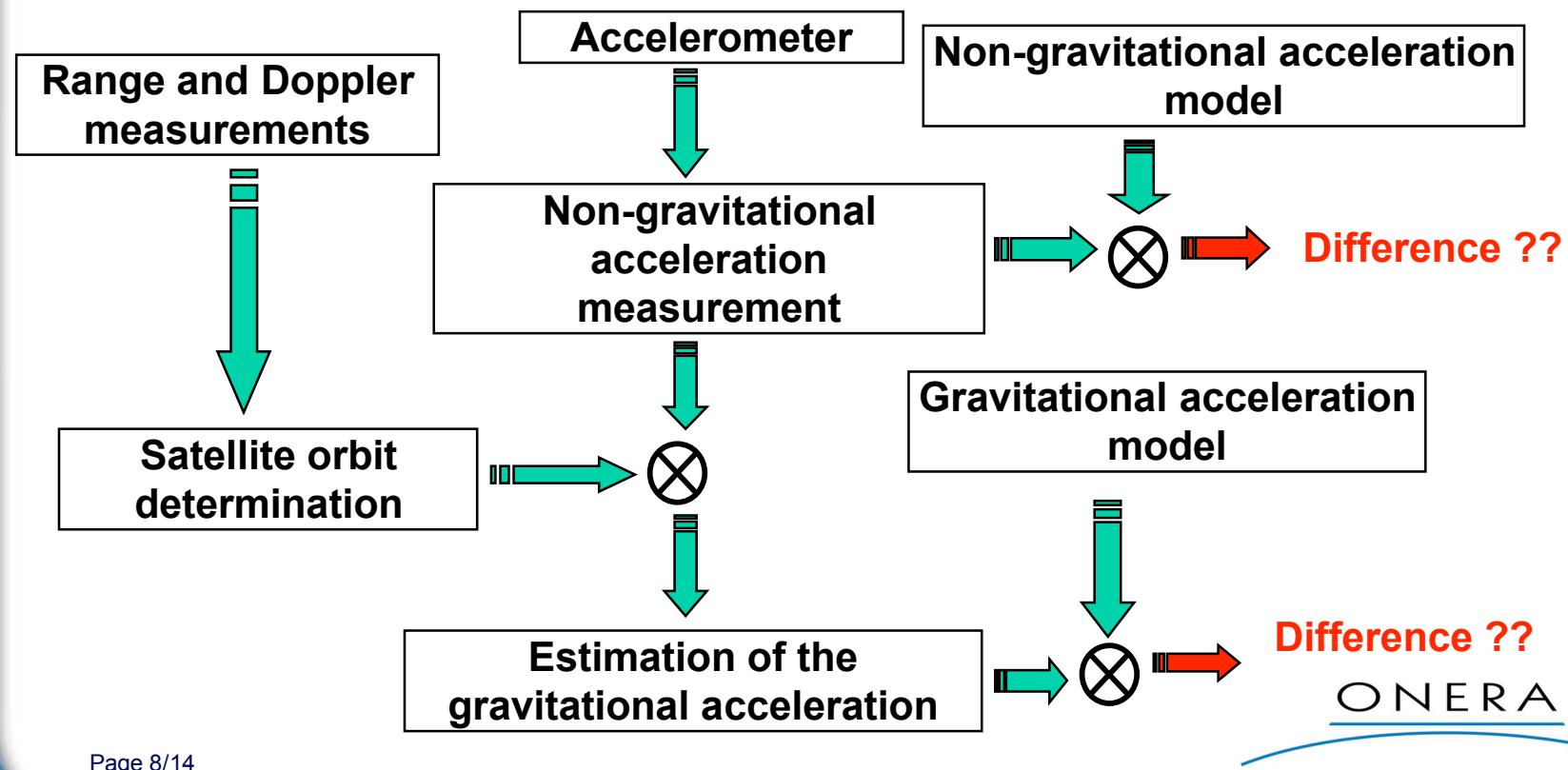
$$\nabla C_2 = -\nabla C_1 = \nabla C \text{ and } V_2 = -V_1 = V$$

$$F = [2\nabla C V_p] V = m[\Gamma - g]$$

Motivation for an accelerometer

Required performance

- Measurement range = depend on the orbit
- Bias $< 10^{-11} \text{ m/s}^2$
- Scale factor *range $< 10^{-11} \text{ m/s}^2$
- Resolution $< 10^{-11} \text{ m/s}^2 \text{ rms}$



Accelerometer performance

Earth Observation: geodesy, geophysics, oceanography, hydrography, climatology

➤ CHAMP (CNES-DLR), July 00

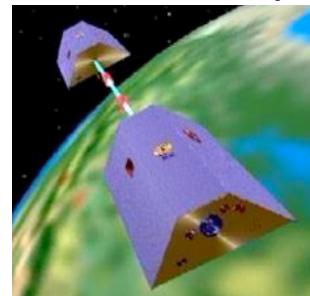


➤ STAR 10^{-3} ms^{-2} - $10^{-8} \text{ ms}^{-2}/\text{Hz}^{1/2}$
 $[10^{-4} - 10^{-1} \text{ Hz}]$

Integration time : 100s → 10^{-9} ms^{-2}



➤ GRACE (NASA-JPL), March 02



➤ SuperSTAR $2.5 \cdot 10^{-5} \text{ ms}^{-2}$ - $10^{-10} \text{ ms}^{-2}/\text{Hz}^{1/2}$
 $[10^{-4} - 4 \cdot 10^{-2} \text{ Hz}]$

Integration time : 100s → 10^{-11} ms^{-2}



➤ GOCE (ESA), 2006-2007

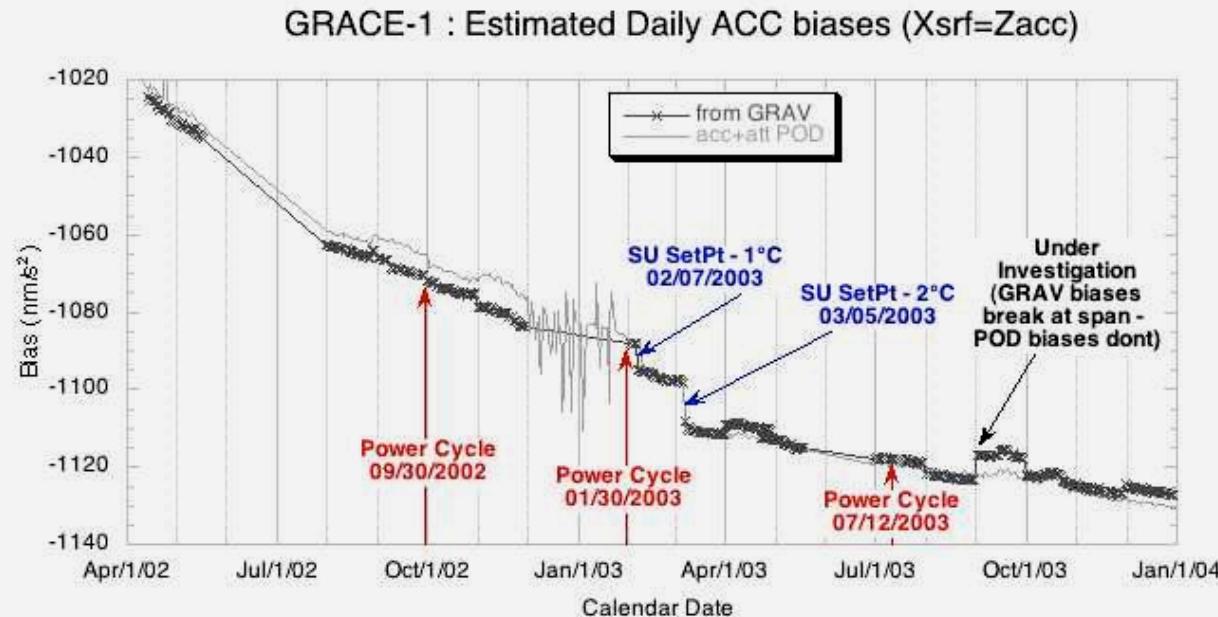


➤ GRADIO
 $6 \cdot 10^{-6} \text{ ms}^{-2}$ - $2 \times 10^{-12} \text{ ms}^{-2}/\text{Hz}^{1/2}$
 $[5 \cdot 10^{-3} - 10^{-1} \text{ Hz}]$

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Evolution of the bias for the GRACE mission

GRACE: SuperSTAR Bias long-term evolution



Linear variation wrt temperature : $\sim 3 \text{ nms}^{-2} / ^\circ\text{C}$

Not sensitive to power cycle

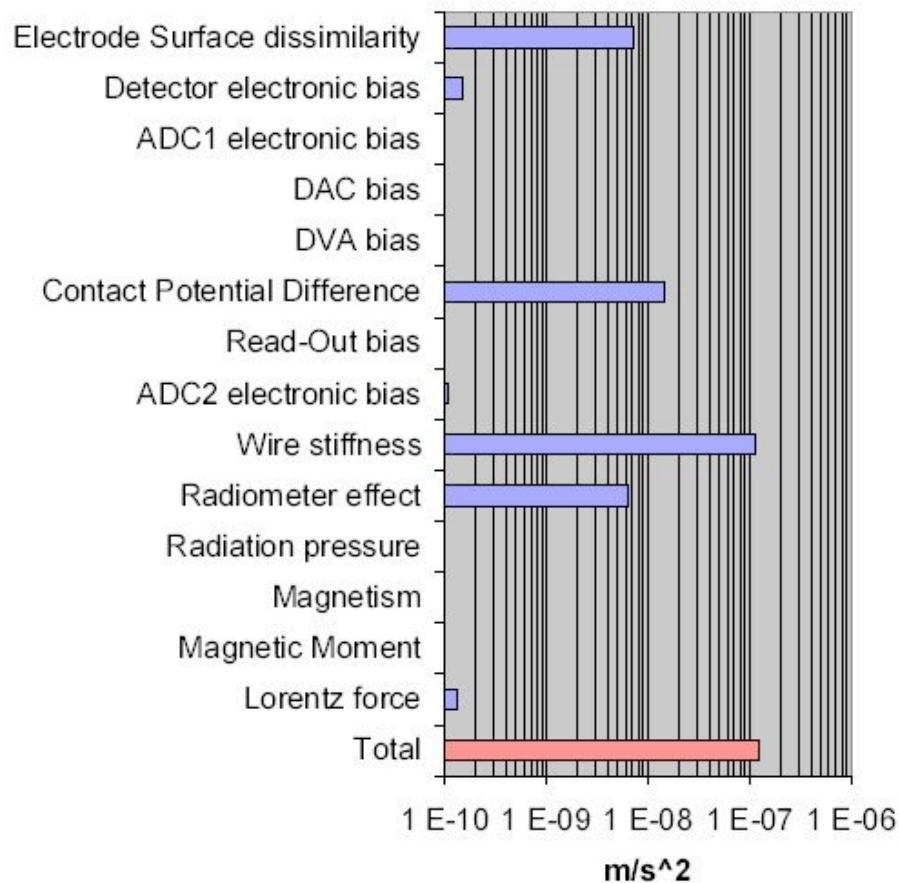
Long term drift : $\sim -20 \text{ nms}^{-2} / \text{year}$

bias to be reduced and/or calibrated in orbit

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Bias for GOCE mission

Y Z bias, Measurement Channel, SCI mode



Contributor	Impact on Measurement Channel Bias (m/s ²)
Electrode Surface dissimilarity	7.03 E-09
Detector electronic bias	1.50 E-10
ADC1 electronic bias	1.20 E-12
DAC bias	0
DVA bias	0
Contact Potential Difference	1.47 E-08
Read-Out bias	4.64 E-11
ADC2 electronic bias	1.08 E-07
Wire stiffness	1.12 E-07
Radiometer effect	6.34 E-09
Radiation pressure	3.50 E-13
Magnetism	2.40 E-13
Magnetic Moment	2.60 E-14
Lorentz force	1.30 E-10
Total	1.25 E-07

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Proposals to suppress the bias

« Null Bias » Accelerometer

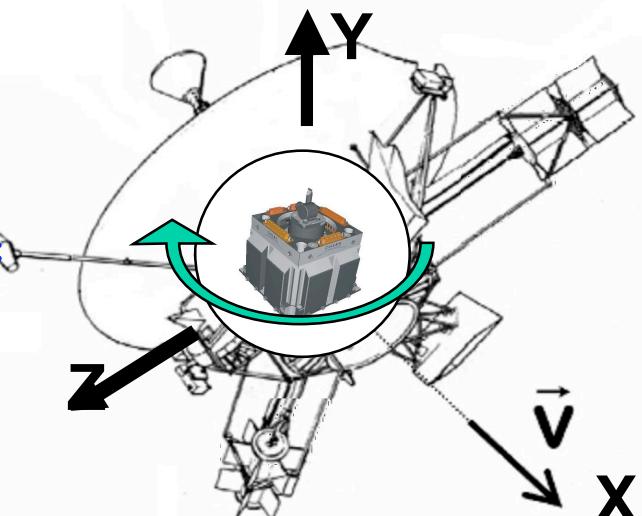
Simple method, Rotate the accelerometer sensitive axes

wrt satellite :

- Calibration with periodic flip during phase measurement

$$M_{1x} = B + (\Gamma - g) \quad \& \quad M_{2x} = B - (\Gamma - g) \rightarrow (\Gamma - g) = 1/2 (M_{1x} - M_{2x})$$

bias stability requirement = flip period



- Modulation method : sine oscillation

Signal about DC shifted @ oscillation frequency, not sensitive to bias instrument

Because of the low and steady drift of the bias :

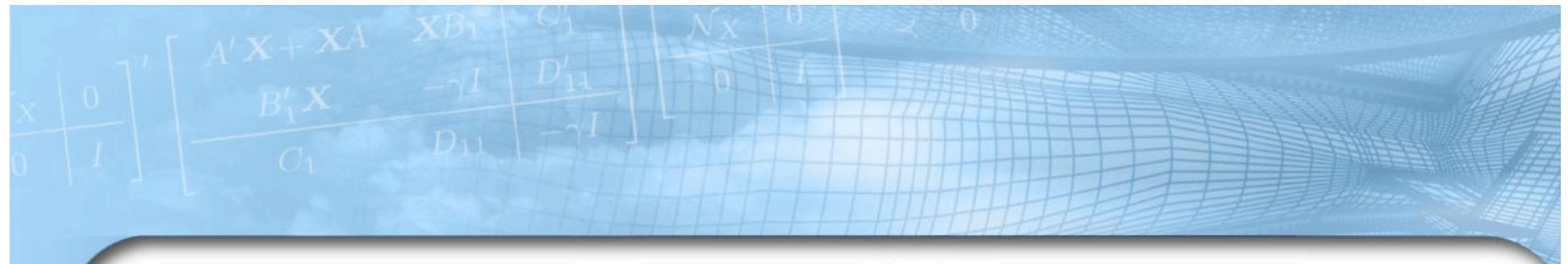
→ periodic calibration sufficient and prefered because of :

- *low power consumption (piezo stepping motor, LISA)*
- *low S/C disturbance (slow motion, balanced moving part wrt rotation axis)*
- *reduced local gravity disturbance (symmetric and balanced device)*

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Conclusion

- With supplemental data, continuation of trajectory analysis and commencement of telemetry analysis
- Future mission necessary to characterize the nature of the Pioneer anomaly
- Accelerometer mandatory to measure the non-gravitationnal acceleration or assess the S/C free fall motion
- Existing ONERA space accelerometers sufficient for Pioneer follow on mission providing the bias is reduced and/or calibrated : under development



ONERA

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Thank you for your attention...

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